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When observing and studying natural processes, we develop mathematical models that describe these phenomena. This modeling introduces errors that are reflected mathematically by perturbed differential equations. A fundamental problem is to determine some type of bound, or “continuous dependence on modeling,” for these errors. We prove Hölder-continuous dependence results for the difference between solutions of certain ill-posed and approximate well-posed inhomogeneous partial differential equations in Hilbert space. Using semigroup theory and operator theoretic methods, we study the inhomogeneous Cauchy problem  $\frac{du}{dt} = Au(t) + h(t)$ ,  $u(0) = \chi$ ,  $0 \leq t < T$ ; where  $A$  is a positive self-adjoint operator on a Hilbert space  $H$ ,  $\chi \in H$ , and  $h : [0, T) \rightarrow H$ . For a suitable function  $f$ , the approximate problem is given by  $\frac{dv}{dt} = f(A)v(t) + h(t)$ ,  $v(0) = \chi$ . Under certain stabilizing conditions, we prove that  $\|u(t) - v(t)\| \leq C\beta^{1-\frac{t}{T}}M^{\frac{t}{T}}$ , where  $C$  and  $M$  are computable constants independent of  $\beta$  and  $0 < \beta < 1$ . These methods are then used to extend our results to Banach space, where  $-A$  is assumed to be the infinitesimal generator of a holomorphic semigroup. (Received September 23, 2005)