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**Donald P. Minassian\*** ([dminassi@butler.edu](mailto:dminassi@butler.edu)), Department of Math. and Actuarial Science,  
Butler University, Indianapolis, IN 46208. *Minimal Axiom Sets for Poisson Processes.*

A Poisson Process  $N$  has been defined traditionally as a counting process (on the nonnegative real axis) satisfying either of the following equivalent axiom sets:

Set A—(1)  $N$  has independent increments, (2) the number of events in any interval  $(s,t]$  is Poisson-distributed with mean  $m(t-s)$ , where  $m>0$  is independent of  $s$  and  $t$ . Set B—(1)  $N$  has independent increments, (2)  $\Pr(1 \text{ event in any interval of length } h) = mh + o(h)$ , (3)  $\Pr(2 \text{ or more events in any interval of length } h) = o(h)$ , where "Pr" is "Probability". For both sets A and B it is often hypothesized that  $N(0)=0$ .

Set A reduces simply to  $\Pr(\text{no events in any interval } (s,t]) = \exp[-m(t-s)]$ ,  $m$  as above, and is independent of events in any nonintersecting interval.

In Set B, (3) reduces to  $\Pr(2 \text{ or more events at any given point}) = 0$ .

The propriety of assuming  $N(0) = 0$  will be discussed. (Received September 16, 2005)