In this talk we give an introduction to level set methods for inverse and optimization problems involving unknown geometries. We construct a gradient flow framework, which finally reduces to appropriate preconditioning of shape gradients for the choice of normal velocities used to move the boundary of the unknown shape towards a solution.

The application to several problems in inverse obstacle reconstruction and shape optimization are also discussed. (Received September 20, 2005)