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Jan P. Boronski* (boronjp@auburn.edu) and **Marian Turzanski**
(mtturz@ux2.math.us.edu.pl). *Antipodal-like theorems and symmetric continua in euclidean spaces.*

We show that for any odd real-valued mapping defined on the euclidean n -cube the set of its zeros contains a unique symmetric component. Such a component separates the n -cube between symmetric points. Additionally, the reverse theorem holds true as well. This is a generalization of the result by Krasinkiewicz, who showed the analogous property for the n -sphere. We discuss also some other theorems concerning the problem of antipodality. Among them, we show that any family of n symmetric continua separating the n -sphere between antipodal points has nonempty intersection, which is equivalent to the Borsuk-Ulam antipodal theorem. Yang's theorem on existence, on the n -sphere, of n orthogonal diameters mapped into a single point is derived from the main theorem. (Received September 14, 2006)