

1023-32-1078

Faruk F Abi Khuzam* (farukakh@aub.edu.lb), American University of Beirut, P.O.Box 11-0236 / Mathematics, Riad El-Solh, Beirut, 1107 2020, Lebanon. *On the growth of vector functions of several complex variables.* Preliminary report.

For meromorphic $f = (f^1, f^2, \dots, f^m) : C^n \rightarrow C^m$, we introduce a “sharp-function” $u_{\max}^{\#}$ as follows: for $z = re^{i\theta}$, $r > 0$, $0 \leq \theta \leq \pi$, put

$$u_{\max}^{\#}(re^{i\theta}, \mathbf{f}) = \max_{1 \leq j \leq m} \sup_{\zeta \in S} u^{\#}(re^{i\theta}, f_{\zeta}^j)$$

where, $u^{\#}(re^{i\theta}, f_{\zeta}^j)$ is the function of Baernstein.

Our simplest results are:

Theorem 1. $u_{\max}^{\#}$ is subharmonic in $\pi^+ = \{z : \text{Im}z > 0\}$, continuous on the closure of π^+ , and:

(a) $u_{\max}^{\#}(r, \mathbf{f}) = N_{\max}(r, \infty, \mathbf{f})$; $u_{\max}^{\#}(re^{i\pi}, \mathbf{f}) = N_{\max}(r, 0, \mathbf{f})$.

(b) $\sup_{0 \leq \theta \leq \pi} u_{\max}^{\#}(re^{i\theta}, \mathbf{f}) = T_{\max}(r, \mathbf{f})$.

Theorem 1. If f is entire of order $\rho \leq 1$, then

$$\limsup_{r \rightarrow \infty} \frac{N_{\max}(r, 0, \mathbf{f})}{\log M(r, \mathbf{f})} \geq \frac{\sin \pi \rho}{\pi \rho}.$$

Furthermore, this inequality is sharp. (Received September 25, 2006)