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Jungho Park* (junjupar@indiana.edu), Department of Mathematics, Rawles Hall, 3rd St.,
Bloomington, IN 47408. *Two-dimensional infinite Prandtl number convection : Structure of
bifurcated solutions.*

We study in this talk the bifurcation, stability and the structure of the bifurcated solutions of two-dimensional infinite Prandtl number convection problem. We prove that the problem bifurcates from the trivial solution to an attractor Σ_R when the Rayleigh number R crosses the first critical Rayleigh number R_c . Concerning the structure of the solutions, we prove that the bifurcated attractor Σ_R consists exactly one cycle of steady state solutions and Σ_R is homeomorphic to S^1 . One of the other main results deals with the structure and its transition of the solutions of the infinite Prandtl number convection in the physical spaces and we prove that the bifurcated solutions are structurally stable. It leads us to the justification of the roll structure for the two-dimensional infinite Prandtl number convection problem as physical experiences suggested. The bifurcation analysis is based on the new bifurcation theory developed by T. Ma and S. Wang called attractor bifurcation. (Received September 26, 2006)