

1023-37-241

**Scot Adams\*** ([adams@math.umn.edu](mailto:adams@math.umn.edu)), School of Mathematics, 127 Vincent Hall, 206 Church St. SE, Minneapolis, MN. *From Lorentzian dynamics to the decay of matrix coefficients.*

The Howe-Moore theorem implies that any ergodic action of a connected noncompact, finite-center, simple Lie group is mixing. Thus, for example, ergodicity inherits to all noncompact closed subgroups, a very useful fact which immediately yields ergodicity of many geometrically-motivated actions. The proofs I know of Howe-Moore go via unitary representation theory. By thinking of a Hilbert space as an infinite-dimensional Riemannian manifold and by adjusting techniques originally used in studying Lorentzian (and Riemannian) dynamics, we can obtain a version of Howe-Moore that is valid for all connected Lie groups, though only useful for nonAbelian groups. Specifically, for any connected Lie group  $G$ , for any faithful irreducible unitary representation of  $G$ , we have: any matrix coefficient tends to zero, as  $Ad(g)$  leaves compact subsets of  $GL(\mathfrak{g})$ , where  $\mathfrak{g}$  is the Lie algebra of  $G$ . (Received August 30, 2006)