

1023-51-558

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Thurston-Bennequin bounds for knots in more general contact manifolds. Preliminary report.

This talk will discuss an integer-valued invariant associated to knots (Y, K) in a contact three-manifold, (Y, ξ) . The invariant, denoted $\tau_\xi(Y, K)$, is a derivative of the knot Floer homology filtration. Under certain assumptions on ξ , we show that $\tau_\xi(Y, K)$ provides upper bounds for the framing numbers of Legendrian representatives of K .

In the case of the standard contact structure on S^3 , $\tau_{\xi_{std}}(S^3, K)$ is denoted $\tau(K)$ and was first defined and studied by Ozsváth and Szabó, and independently by Rasmussen. Plamenevskaya discovered a connection between $\tau(K)$ and the framing invariants of Legendrian representatives of K . Specifically, she showed:

$$tb(\tilde{K}) + |rot(\tilde{K})| \leq 2\tau(K) - 1,$$

where \tilde{K} is any Legendrian realization of K . Here tb and rot denote the Thurston-Bennequin and rotation numbers of \tilde{K} , respectively.

We will show that $\tau_\xi(Y, K)$ satisfies an analogous inequality. We will then present several applications. One such application uses $\tau_\xi(Y, K)$ to obstruct a knot (Y, K) from arising as the boundary of a properly embedded J -holomorphic curve, V , in a symplectic filling of (Y, ξ) i.e. $(Y, K, \xi) = \partial(W, V, \omega)$. (Received September 18, 2006)