The mapping class group of a Heegaard splitting is the group of automorphisms of the ambient manifold that take the Heegaard surface onto itself. I will discuss results concerning finite subgroups of the mapping class group and elements that are non-trivial in the Heegaard surface but isotopic to the identity in the ambient manifold. (Received September 22, 2006)