

1023-60-926

Aurel Iulian Stan* (stan.7@osu.edu), 1465 Mount Vernon Avenue, Marion, OH 43302. *Best constants in norms of non-gaussian Wick products*. Preliminary report.

It is known that, if X is a normally distributed random variable, then for any polynomials f and g , and any positive numbers p and q , such that $(1/p) + (1/q) = 1$, the following inequality holds:

$$E[|f(X) \diamond g(X)|^2] \leq E[|\Gamma(\sqrt{p}I)f(X)|^2]E[|\Gamma(\sqrt{q}I)g(X)|^2],$$

where, for any complex number c , $\Gamma(cI)$ denotes the second quantization operator of c times the identity operator I , $f(X) \diamond g(X)$ the Wick product of $f(X)$ and $g(X)$, and $E[\cdot]$ the expectation. Moreover, the following inequality also holds:

$$E[|f(X) \diamond g(X)|^2] \leq \binom{m+n}{m} E[|f(X)|^2]E[|g(X)|^2],$$

where m and n denote the degrees of the polynomials f and g , respectively. We will show that the first inequality can be extended to all non-gaussian random variables X , having finite moments of any order, whose Szegő-Jacobi omega sequence is sub-additive, while the second inequality can be generalized to all random variables for which the omega sequence is super-additive. (Received September 23, 2006)