

1035-03-266

Jan Reimann*, University of California Berkeley, Department of Mathematics, 705 Evans Hall, Berkeley, CA 94707. *Measures and their random reals.*

The duality between measures and the sets they “charge” is a central theme in modern analysis. An effective analogue of this question is: Given a real x , does there exist a (probability) measure relative to which x is effectively random (so that x is not an atom of the measure)? And if such a measure exists, can we ensure that it has certain properties (non-atomic, of a certain minimum capacity, etc)? While every non-computable real is random with respect to some measure, there exists a nested sequence of countable Π_1^1 sets of reals that are not n -random with respect to any continuous measure. This sequence exhibits a number of interesting properties. For instance, the proof that all of the sets are countable requires the existence of infinitely many iterates of the power set of ω , similar to Borel determinacy. Furthermore, there does not seem to be a natural notion of rank for such reals.

I will first survey the basic results on continuous randomness, before discussing more recent results on continuous 1-randomness. The techniques used in the proofs are drawn from various areas of logic and analysis, such as Turing degrees, Π_0^1 classes, determinacy, fine structure, or Hausdorff measures. (Received September 12, 2007)