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Victor O. Larsen* (vlarsen@middlebury.edu), 3501 Middlebury College, Middlebury, VT 05753. *A Tree with Maximum Degree Three and Game Chromatic Number Four*. Preliminary report.

We examine the following coloring game played on a graph G . Given a fixed positive integer r , Alice and Bob alternately color the vertices of G with r colors. Alice makes the first move. The game ends when no more vertices can be legally colored. A color α is legal for a vertex u if no neighbors of u are colored with α . If the entire graph is eventually colored, Alice wins. If there exists any uncolored vertex with no legal color, then Bob wins. The least r such that Alice has a winning strategy is called the game chromatic number of G . This parameter has been examined in many other papers, and it has been proven that every tree has game chromatic number at most 4. We show that there exists a tree with maximum degree 3 on which Alice does not have a winning strategy using only 3 colors. This proves that there exists a tree with maximum degree 3 and game chromatic number 4. (Received August 07, 2008)