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Sherry Gong*, Cabot Mail Center Box #291, Cambridge, MA 02138. *On a Conjecture Regarding the Coefficients of Cyclotomic Polynomials.*

Let $a_n(k)$ be the coefficient of x^k in the n th cyclotomic polynomial

$$\Phi_n(x) = \prod_{\substack{j=1 \\ \gcd(j,n)=1}}^n (x - e^{\frac{2\pi j i}{n}})$$

Let $M(a_n(k)) = \lim_{x \rightarrow \infty} \frac{1}{x} \sum_{n \leq x} a_n(k)$ be the average of $a_n(k)$, as introduced by Möller, and let

$$f_k = \frac{\pi^2}{6} M(a_n(k)) k \prod_{\substack{q \leq k \\ q \text{ prime}}} (q + 1).$$

It was conjectured by Y. Gallot, P. Moree and H. Hommersom that the f_k are integers for all k . In this paper, we prove this conjecture. Moreover, we show that for any fixed natural number n , f_k contains n as a factor for sufficiently large k . (Received September 15, 2008)