Let $S$ be closed oriented surface of genus $\sigma$ and let $N_\sigma$ be the number of distinct topological finite non-trivial group actions on $S$. For general $\sigma$, it is easy to determine a bound for $N_\sigma$, but such a bound is usually a gross over approximation. We consider the problem of refining such a bound. (Received September 05, 2008)