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Let  $\Omega \subset \mathbb{R}^n$  be a bounded Lipschitz domain, whose boundary decomposes into two disjoint pieces  $\Sigma_t, \Sigma_n \subseteq \partial\Omega$ , which meet at an angle  $< \pi$ . Denote by  $\nu$  the outward unit normal to  $\Omega$ . Then there exists  $\varepsilon > 0$  with the property that if  $|2 - p| < \varepsilon$  then the following holds. Consider a vector field  $u$  with components  $u_1, \dots, u_n \in L^p(\Omega)$  such that  $\operatorname{div} u = \sum_{j=1}^n \partial_j u_j \in L^p(\Omega)$  and  $\operatorname{curl} u = (\partial_j u_k - \partial_k u_j)_{1 \leq j, k \leq n} \in L^p(\Omega)$ . Set  $\nu \cdot u = \sum_{j=1}^n \nu_j u_j$  and  $\nu \times u = (\nu_j u_k - \nu_k u_j)_{1 \leq j, k \leq n}$ . Then the following are equivalent:

- (i)  $(\nu \cdot u)|_{\Sigma_t} \in L^p(\Sigma_t)$  and  $(\nu \times u)|_{\Sigma_n} \in L^p(\Sigma_n)$ ;
- (ii)  $\nu \cdot u \in L^p(\partial\Omega)$ ;
- (iii)  $\nu \times u \in L^p(\partial\Omega)$ .

This generalizes earlier work dealing with the case when  $\Sigma_t = \emptyset$  or  $\Sigma_n = \emptyset$ . (Received August 19, 2008)