New constructive and non-constructive non-asymptotic uniform error bounds for approximating functions in $L^2_s(\mathbb{R}^d)$, $d \geq 1$, by finite compactly supported multiresolution expansions are proved using approximation theoretic bounds derived from statistical learning theory. (Received September 04, 2008)