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**R KillGrove\***, 2041 W. Vista Way 7245, Vista, CA 92083, and **L Taylor** and **D Koster**. *Two Neat Results In Elementary Geometry*.

Axioms of an ordered plane use the ternary relation  $\omega ABC$ , eg. *Self-Dual Confined Configurations With Ten Points*, **Ars Comb** **67** (2003) 37–63. In  $E^2$  for  $A:(A_1, A_2)$  and  $C:(C_1, C_2)$  with  $A \neq C$  and  $B:(B_1, B_2)$  satisfy  $\omega ABC$  iff  $\exists t, 0 < t < 1$   $\ni$  for  $i=1,2$   $B_i = tA_i + (1-t)C_i$ . For  $\triangle P_1P_2P_3$  (triangle  $P_1P_2P_3$ ) and let  $\triangle Q_1Q_2Q_3$  be where  $\omega P_1Q_3P_2$ ,  $\omega P_2Q_1P_3$ , and  $\omega P_3Q_2P_1$  using the same  $t$ . Special case:  $A:(u, v)$ ,  $0 < u < 1$ ,  $v > 0$ ,  $B:(0, 0)$ ,  $C:(1, 0)$ ,  $A':(1-t, 0)$ ,  $B':(t + (1-t)u, (1-t)v)$   $C':(tu, tv)$ . The charm: areas of  $\triangle AB'C'$ ,  $\triangle A'BC'$ , and  $\triangle A'B'C$  are equal. Koster has shown finite field planes (analytic geometry in the field) whose orders are congruent to 2 mod 3, except 2, satisfy all the axioms of an ordered plane except the Pasch axiom. These are ordered planes even though their defining fields are not ordered. (Received September 10, 2008)