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**John Shareshian.** *Non-right-orderable 3-manifold groups.*

We investigate the orderability of fundamental groups of 3-manifolds. We restrict attention to groups of the form

$$G = \langle t, a, b \mid a^t = a^{\phi_*}, b^t = b^{\phi_*}, t^p [a, b]^q = 1 \rangle,$$

where  $\phi_*$  is any automorphism of the rank two free group  $F = F(a, b)$  such that

- $[a, b]^{\phi_*} = [a, b]$ , and
- the automorphism  $\phi_{\sharp}$  of the abelianization  $F/[F, F] \cong \mathbb{Z} \oplus \mathbb{Z}$  induced by  $\phi_*$  lies in  $SL_2(\mathbb{Z})$ , with  $|\text{Trace}(\phi_{\sharp})| > 2$ .

In other words,  $\phi_*$  is induced by an orientation preserving pseudo-Anosov homeomorphism  $\phi$  of a once punctured torus. We show that if either  $\text{Trace}(\phi_{\sharp}) < -2$  and  $\frac{p}{q} \in [1, \infty]$  or  $\text{Trace}(\phi_{\sharp}) > 2$  and  $(p, q) = (1, 0)$  then  $G(\phi, p, q)$  is not right orderable.

There is some overlap between this work and the work of Dąbkowski, Przytycki and Togha. (Received September 16, 2008)