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**Ala' Jamil Alnaser\*** (alnaser@math.ksu.edu), Department of Mathematics, Kansas State University, Manhattan, KS 66502. *Waring's Problem in Number Fields*. Preliminary report.

Let  $p$  be an odd prime and  $\gamma(k, p^n)$  be the smallest positive integer  $s$  such that every integer is a sum of  $s$   $k$ -th powers (mod  $p^n$ ). Earlier we established  $\gamma(k, p^n) \leq [k/2] + 2$  and  $\gamma(k, p^n) \ll \sqrt{k}$  provided that  $k$  is not divisible by  $(p-1)/2$ . Also if  $t = (p-1)/(p-1, k)$ , and  $q$  is any positive integer, we showed that if  $\phi(t) \geq q$  then  $\gamma(k, p^n) \leq c(q)k^{1/q}$  for some constant  $c(q)$ . These results generalized results known for the case of prime moduli. Here we generalize these results to a number field setting. Let  $F$  be a number field,  $R$  its ring of integers and  $P$  a prime ideal in  $R$  that lies over a rational prime  $p$  with degree of inertia  $f$ . Let  $\gamma(k, P^n)$  be the smallest integer  $s$  such that every algebraic integer in  $F$  that can be expressed as a sum of  $k$ -th powers (mod  $P^n$ ) is expressible as a sum of  $s$   $k$ -th powers (mod  $P^n$ ). We prove for instance that when  $t = (p^f - 1)/(p - 1, k)$  then  $\gamma(k, P^n) \leq c(t)p^{nf/\phi(t)}$ . (Received September 16, 2008)