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We consider a Tic-Tac-Toe game played on the  $d$ -dimensional integer lattice. The game that we investigate is a Maker-Breaker version of Tic-Tac-Toe. In a Maker-Breaker game, the first player, Maker, only tries to occupy a winning line and the second player, Breaker, only tries to stop Maker from occupying a winning line. We consider the bounded number of directions game, in which we designate a finite set of direction-vectors  $\mathcal{S} \subset \mathbb{Z}^d$  which determines the set of winning lines. We show that Maker can build winning lines of length up to  $(1 + o(1))d \lg k$  if  $\mathcal{S}$  is the set of *all* direction-vectors with coordinates bounded by  $k$ . We also apply similar methods to the  $n$ -consecutive lattice points game on the  $N^d$  board with (essentially)  $\mathcal{S} = \mathbb{Z}^d$ , and we show that the phase transition from a win for Maker to a win for Breaker occurs at  $n = (d + o(1)) \lg N$ . (Received September 22, 2009)