A number field is said to be monogenic if its ring of integers is a simple ring extension $\mathbb{Z}[\alpha]$ of $\mathbb{Z}$. It is a classical and usually difficult problem to determine whether a given number field is monogenic, and if it is, to find all numbers $\alpha$ that generate a power integral basis $\{1, \alpha, \alpha^2, \ldots, \alpha^k\}$ for the ring. We consider cyclotomic fields, which are known to be monogenic, and by studying units in the ring arrive at a conjectural solution to the problem of finding all the power integral bases for these fields. G. Ranieri recently proved that if $L = \mathbb{Q}(\zeta_n)$ is a cyclotomic field whose conductor $n$ is relatively prime to 6, then up to integer translation all the generators lie on the unit circle or the line $\text{Re}(z) = 1/2$ in the complex plane. We prove that this interesting geometric restriction extends to the cases of conductor $n = 3k$ and $n = 4k$, where $k$ is relatively prime to 6. We use this result to find all power integral bases for $\mathbb{Q}(\zeta_n)$ for $n = 15, 20, 21, 28$, and so verify our conjecture in these cases. (Received September 22, 2009)