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The partial Noether operators and partial Euler-Lagrange equations are developed for a single as well as for a system of  $k$ th-order ordinary differential equations (ODEs) in the complex domain with the help of complex partial Lagrangians. A complex partial Noether theorem is deduced and the formula which provides the complex first integral is equivalent to the complex Noether integral. These complex partial Noether operators, in general, are not complex symmetries of systems of complex ODEs and they are not closed. The theorems are provided which give the condition of closure and when they become complex symmetry generators is also stated. The results obtained in the complex domain are decomposed into the real domain for system of  $m$  second-order complex ODEs with  $m$  dependent variables. The complex partial Lagrangian splits into two real partial Lagrangians which satisfy partial Euler-Lagrange equations in the real domain. Each complex partial Noether operator yields two real partial Noether operators of the real partial Lagrangians. The complex first integrals result in two real first integrals for the system of ODEs split in the real domain. (Received September 06, 2009)