

We prove Hölder-continuous dependence results for the difference between certain ill-posed and well-posed evolution problems in a Banach space  $X$ . We consider the ill-posed evolution problem

$$\begin{aligned} \frac{du(t)}{dt} &= A(t, D)u(t) & 0 \leq t < T \\ u(0) &= \chi, \end{aligned} \tag{1}$$

where  $iD$  is the generator of a bounded strongly continuous group on  $X$ , and  $A(t, D) = \sum_{j=1}^k a_j(t)D^j$  with  $a_j \in C([0, T] : \mathbb{C})$  for each  $1 \leq j \leq k$ . We determine families  $\{f(t, D)\}_{t \in [0, T]}$  of operators in  $X$  such that the problem

$$\begin{aligned} \frac{dv(t)}{dt} &= f(t, D)v(t) & 0 \leq t < T \\ v(0) &= \chi \end{aligned} \tag{2}$$

is well-posed and such that solutions of the well-posed problem (2) approximate known solutions of the original ill-posed problem (1). We use  $C$ -regularized evolution systems to obtain our approximation which establishes continuous dependence on modeling for the problems under consideration. Namely, assuming  $u(t)$  and  $v(t)$  are solutions of (1) and (2) respectively, we prove that

$$\|u(t) - v(t)\|_1 \leq C_1 \beta^{1 - \frac{t}{T}} M^{\frac{t}{T}}$$

for a suitable norm  $\|\cdot\|_1$ , where  $0 < \beta < 1$ , and  $C_1$  and  $M$  are constants independent of  $\beta$ . (Received September 21, 2009)