

1056-47-110

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For a large class of admissible scalar functions  $f$ , we obtain scalar integral representations for operator derivatives  $\frac{d^k}{dt^k} f(H_0 + tV)$  inside a normal faithful semi-finite trace  $\tau$ , with an initial operator  $H_0$  belonging to a semi-finite von Neumann algebra  $\mathcal{A}$ , an increment  $V$  to a  $\tau$ -Hilbert-Schmidt class of  $\mathcal{A}$ , and the values of  $k$  determined by further properties of  $\mathcal{A}$ . These representations imply, in particular, that computation of  $\tau \left[ \frac{d^k}{dt^k} f(H_0 + tV) \right]$  can be reduced to the computation of  $\frac{d^{k-1}}{dt^{k-1}} f'(H_0 + tV)$  and that the remainder of a Taylor-type approximation  $\tau \left[ f(H_0 + V) - \sum_{k=0}^{p-1} \frac{1}{k!} \frac{d^k}{dt^k} \Big|_{t=0} f(H_0 + tV) \right]$  is a bounded functional on  $f^{(p)}$ . (Received July 27, 2009)