

1056-49-44

**Nasiruddin U Ahmed\*** (ahmed@site.uottawa.ca), 800 King Edward Str., Ottawa, Ontario K1N6N5, Canada. *Operator Valued Measures as Feedback Control for Stochastic Systems on Hilbert Space.*

We consider a partially observed stochastic control problem with operator valued measures as controls. This is given by the following stochastic differential equation on the Hilbert space  $X$  coupled with an algebraic equation representing noisy measurement process taking values from another Hilbert space  $Y$  as follows:

$$dx = Axdt + B(dt)y(t-) + \sigma(t)dW(t), t \in I \equiv [0, T], x(0) = x_0 \quad (1)$$

$$y(t) = C(t)x(t) + \xi(t), t \in I. \quad (2)$$

The process  $x$  is the state,  $y$  is the observation and  $W$  is a Brownian motion taking values from a Hilbert space  $H$  and  $\xi$  is an arbitrary second order  $Y$  valued random processes. The operator  $A$  is the generator of a  $C_0$ -semigroup of bounded linear operators on  $X$ ,  $B \in M_{cabv}(\Sigma, \mathcal{L}(Y, X))$  and  $\sigma \in B_\infty(I, \mathcal{L}(H, X))$ . The problem is to find a control policy  $B \in \Gamma \subset M_{cabv}(\Sigma, \mathcal{L}(Y, X))$  that minimizes the functional

$$J(B) \equiv \int_I Tr(P(t)) \lambda(dt) + \int_I |\bar{x}(t) - x_d(t)|_X^2 \nu(dt) + \Phi(B), \quad (3)$$

where  $P(t)$ , dependent on  $B$ , is the covariance operator taking values from the space of nuclear operators  $\mathcal{L}_1(X)$  and  $\lambda$  and  $\nu$  are nonnegative measures. (Received July 09, 2009)