We present a combinatorial proof of an identity for the odd Fibonacci numbers $F_{2n+1}$ by counting the number of collections of mutually disjoint convex subsets of a totally ordered set of $n$ points. We discuss how the problem is motivated by counting certain topologies on finite sets, and relate it to Pascal’s triangle. (Received September 21, 2009)