

1067-03-679

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An *integer part*  $I$  for an ordered field  $R$  is a discrete ordered subring containing 1 such that for all  $r \in R$  there exists a unique  $i \in I$  with  $i \leq r < i + 1$ . Mourgues and Ressayre showed that every real closed field  $R$  has an integer part. Let  $k$  be the residue field of  $R$ , and let  $G$  be the value group of  $R$ . Let  $k\langle\langle G \rangle\rangle$  be the set of *generalized power series* of the form  $\sum_{g \in S} a_g g$  where  $a_g \in k$  and the support of the power series  $S \subseteq G$  is well ordered. Mourgues and Ressayre produce an integer part for  $R$  by building a special embedding of  $R$  into  $k\langle\langle G \rangle\rangle$ . To understand the complexity of integer parts, we analyzed an algorithmic version of their construction for countable  $R$  and showed that the generalized power series in the image of  $R$  are of length less than  $\omega^{\omega^\omega}$ . Ressayre showed that every real closed exponential field has an integer part that is closed under  $2^x$  using the same approach. However, he had to more carefully choose the value group  $G$  and the embedding of  $R$  into  $k\langle\langle G \rangle\rangle$ . We explore how these alterations affect the lengths of the generalized power series in the image of  $R$ . (Received September 13, 2010)