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Sibel Ozkan (sozkan@mtu.edu) and **Erik E Westlund*** (erik.westlund@uwc.edu). *Hall m -completable graphs*. Preliminary report.

A partial proper m -coloring of a graph G is a proper coloring $\varphi : V_0 \rightarrow \{1, \dots, m\}$, for some $V_0 \subseteq V(G)$. Define the list-assignment $L = L_\varphi$ by $L(v) = \{\varphi(v)\}$ if $v \in V_0$, and $L(v) = \{1, \dots, m\} \setminus \{\varphi(N_G(v) \cap V_0)\}$ if $v \in V \setminus V_0$, where $N_G(v)$ denotes the neighborhood of v . φ has a completion to a proper m -coloring of G if and only if G has a proper L_φ -coloring. We say (G, L) satisfies Hall's condition if, for all subgraphs H of G , $|V(H)| \leq \sum_{\sigma \in \mathcal{C}} \alpha(H(\sigma, L))$, where $\alpha(H(\sigma, L))$ is the independence number of the subgraph of H induced on the vertices having σ in their lists. Hall's condition is necessary for G to have a proper L -coloring. G is said to be Hall m -completable, for some $m \geq \chi(G)$, if ever partial proper m -coloring φ , such that (G, L_φ) satisfies Hall's condition, has a completion. In this talk, we discuss new results in classifying Hall m -completable graphs for certain values of m . (Received September 21, 2010)