

1067-05-805

Ryan K Therkelsen* (rtherkelsen@bellarmine.edu), Mathematics Department, Bellarmine University, 2001 Newburg Road, Louisville, KY 40205. *Order in the Conjugacy Decomposition of the Rook Monoid*. Preliminary report.

The rook monoid R_n consists of the $(0, 1)$ -matrices of size n , having at most one non-zero entry in each row and each column. The Gauss-Jordan elements \mathcal{GJ} of R_n are those elements in reduced row echelon form. Our object of study is the partially ordered set \mathcal{P} whose elements are the conjugacy classes of \mathcal{GJ} with a partial order defined in terms of a generalized dominance order on partitions of m , for $0 \leq m \leq n$. We present a new decomposition of \mathcal{P} , in terms of partitions, that we use to describe an order-preserving map between elements in \mathcal{P} whose representatives have different rank. Analogous maps have been found for R_n that provide insight into its structure, under the Bruhat-Chevalley order. Time permitting, we will comment on how \mathcal{P} fits in with a decomposition of $M_n(k)$ related to conjugacy classes. (Received September 15, 2010)