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Subsets of $1, 2, 3, \dots, n$.*

For $n > 0$ let $[n] = 1, 2, 3, \dots, n$. A subset S of $[n]$ is called extraordinary if the size of S equals the minimal element in S . The number of extraordinary subsets of $[n]$ is F_n , the n th Fibonacci number. For these subsets, one can count (i) the total number of elements, with repeats considered, that appear in all the extraordinary subsets of $[n]$, and (ii) the sum of all the elements that appear among the extraordinary subsets. Fixing $n > 0$, for $1 \leq k \leq n$, we consider $a(n, k)$ which counts the number of extraordinary subsets of $[n]$ that contain k . We find that the sequence $a(n, k)$ is unimodal and discover the Catalan numbers when studying these unimodal sequences. (Received September 15, 2010)