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John H. Johnson* (johnsojh@dukes.jmu.edu). *J-sets in Commutative and Uncommutative Semigroups.*

A J -set in \mathbb{N} enjoys an easily derived combinatorial property:

Given a sequence $\langle x_n \rangle_{n=1}^{\infty}$ in \mathbb{N} , a J -set in \mathbb{N} contains arbitrarily long arithmetic progressions with difference from $\{ \sum_{n \in F} x_n : \emptyset \neq F \subseteq \mathbb{N} \text{ is finite} \}$.

It's also a (not so easily derived) fact that every set with positive upper density is a J -set in \mathbb{N} . The notion of a J -set makes sense in any semigroup, and it is from this context we will look at J -sets. In this talk we will show the following result.

Proposition. *Let S be a commutative semigroup, $T \subseteq S$ a subsemigroup, and $A \subseteq T$. If A is a J -set in S , then A is a J -set in T .*

We will also show that this Proposition is false when the commutativity assumption is dropped. (Received September 18, 2010)