Two irreducible polynomials over $F_2$ are called *twins* provided they differ only in their linear and quadratic coefficients. The aim of this research is to prove that there are infinitely many twin irreducible polynomials over $F_2$. Though no proof has yet been achieved, we outline here several promising conjectures toward this end. (Received September 20, 2010)