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**Dian Yang\*** (yangd1989@gmail.com), CSU 4062, PO Box 8793, College of William and Mary,  
Williamsburg, VA 23186. *Solution Theory for Bilinear Systems of Equations.*

For  $A_1, \dots, A_m \in M_{p,q}(\mathbb{F})$  and  $g \in \mathbb{F}^m$ , any system of equations of the form  $y^T A_i x = g_i$ ,  $i = 1, \dots, m$ , with  $y$  varying over  $\mathbb{F}^p$  and  $x$  varying over  $\mathbb{F}^q$  is called bilinear. A solution theory for complete systems ( $m = pq$ ) is given in [JL]. Given here is a general solution theory for bilinear system of equations. In particular we prove that the problem of solving a bilinear system is equivalent to finding rank one points of an affine matrix function. For this, we notice a relationship between bilinear systems and linear systems. We also study systems with certain left hand side matrices  $\{A_i\}_{i=1}^m$  such that a solution exist no matter what right hand side  $g$  is. A criterion is given to distinguish such  $\{A_i\}_{i=1}^m$ .

[JL] C. R. Johnson and J. A. Link, *Solution theory for complete bilinear systems of equations*, Numerical Linear Algebra with Applications, **16** No.11-12 (2009), pages 929–934. (Received August 14, 2010)