We study the $H^\infty(\mathbb{B}_n)$ Corona problem $\sum_{j=1}^{N} f_j g_j = h$ and show it is always possible to find solutions $f$ that belong to $BMOA(\mathbb{B}_n)$ for any $n > 1$, including infinitely many generators $N$. Our method of proof is to solve $\overline{\partial}$-problems and to exploit the connection between $BMO$ functions and Carleson measures for $H^2(\mathbb{B}_n)$. Key to this is the exact structure of the kernels that solve the $\overline{\partial}$ equation for $(0, q)$ forms, as well as new estimates for iterates of these operators. A generalization to multiplier algebras of Besov-Sobolev spaces is also given. (Received September 08, 2010)