

1067-AB-1446 **Alexander E Holroyd*** (holroyd@microsoft.com). *Random Sorting*.

See <http://research.microsoft.com/holroyd/sort/> for pictures.

Sorting a list of items is among the most celebrated of algorithmic problems. If one must do this by swapping neighboring pairs, the worst initial condition is when the n items are in reverse order, in which case n choose 2 swaps are needed. A sorting network is any sequence of n choose 2 swaps which achieves this.

This seemingly simple concept reveals amazing new structure when an element of randomness is introduced. Specifically, choose an n -item sorting network uniformly at random. It is conjectured that, in limit $n \rightarrow$ infinity, the trajectories of individual items are random Sine curves, while the half-time permutation matrix concentrates in a circular disc. These conjectures are overwhelmingly supported by simulation evidence, consistent (but weaker) rigorous results, and an extremely plausible geometric picture. I will explain all this with the help of visual demonstrations. No prior knowledge will be assumed.

Based on joint works with O. Angel, V. Gorin, D. Romik, and B. Vira (Received September 21, 2010)