962-05-1398

Silvia P Heubach* (sheubac@calstatela.edu), Dept. of Mathematics and Computer Science, California State University Los Angeles, 5151 State University Drive, Los Angeles, CA 90032-8204, and Phyllis Z Chinn. Exact and Asymptotic Results for Tilings of Rectangles with Squares.

The authors have derived exact and asymptotic results for the number of tilings, $T_{m,n}$, of an $m \times n$ area with 1×1 and 2×2 tiles. In particular, the focus is on $T_{m,n}^k$, the number of such tilings which contain exactly k of the 2×2 tiles. For m=2 and m=3, exact results have been established for $T_{m,n}^k$. For m=4 and m=5, recursions for $T_{m,n}^k$ were derived and used to compute the generating functions $G_m(x,t) := \sum_{n,k\geq 0} T_{m,n}^k x^n t^k$ and $G_m(x) := \sum_{n\geq 0} T_{m,n} x^n$ for $T_{m,n}^k$ and $T_{m,n}$, respectively. Asymptotic behavior for $T_{m,n}^k$ and $T_{m,n}$ is then obtained from the respective generating functions. (Received October 03, 2000)