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Every  $\text{low}_n$  Boolean algebra, for  $1 \leq n \leq 4$ , is isomorphic to a computable Boolean algebra. It is not yet known whether the same is true for  $n > 4$ . However, it is known that there exists a  $\text{low}_5$  subalgebra of the computable atomless Boolean algebra which, when viewed as a relation on the computable atomless Boolean algebra, does not have a computable copy. We adapt the proof of this recent result to show that there exists a  $\text{low}_4$  subalgebra of the computable atomless Boolean algebra which, when viewed as a relation on the computable atomless Boolean algebra, has no computable copy. This result provides a sharp contrast with the one which shows that every  $\text{low}_4$  Boolean algebra has a computable copy. That is, the spectrum of the subalgebra as a unary relation can contain a  $\text{low}_4$  degree without containing the degree  $\mathbf{0}$ , even though no spectrum of a Boolean algebra (viewed as a structure) can do the same. (Received September 03, 2011)