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Keivan Hassani Monfared* (k1monfared@gmail.com), 1103 E CANBY ST., Laramie, WY 82072. *On the Permanent Rank of Matrices.*

The permanent of the $n \times n$ matrix $A = [a_{ij}]$ is defined to be the sum of all diagonal products of A , that is:

$$\text{per}(A) = \sum_{\sigma \in S_n} \prod_{i=1}^n a_{i\sigma(i)},$$

where S_n is the symmetric group of order n .

The term rank of A , denoted $\text{termrank}(A)$, is the largest number of nonzero entries of A with no two in the same row or column. The permanent rank of a matrix A , denoted by $\text{perrank}(A)$, is defined to be the size of a largest square sub-matrix of A with nonzero permanent.

Here we study the following conjecture relating the perrank and the termrank:

Conjecture: For any matrix A ,

$$\text{perrank}(A) \geq \left\lceil \frac{\text{termrank}(A)}{2} \right\rceil,$$

and for even termrank the equality holds if and only if $A = \bigoplus \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$, up to permutation and scaling of rows and columns of A , and omitting zero rows and columns.

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