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We consider the problem of counting decompositions of r -additive (or linearized) polynomials over a finite field \mathbb{F}_q , for q a power of a prime power r . The r -additive polynomials in $\mathbb{F}_q[x]$ have the form $f = \sum_{0 \leq i \leq d} f_i x^{r^i}$. We count the number of distinct functional decompositions of r -additive polynomials with a right component of degree r :

$$C(f) = \# \{a \in \mathbb{F}_q : f = g \circ (x^r + ax)\},$$
$$R(d) = \{C(f) : f \in \mathbb{F}_q[x] \text{ monic, squarefree, } r\text{-additive of degree } r^d\}.$$

We determine $R(d)$ for all d , and in particular $R(2) = \{0, 1, 2, r + 1\}$ and $R(3) = \{0, 1, 2, 3, r + 1, r + 2, r^2 + r + 1\}$. For $R(2)$ this is consistent with the work of Blüher (2004), who also considers the inverse problem of finding formulas for the number of polynomials in each class. I.e., for given d find

$$A_i^{(d)} = \# \{f \in \mathbb{F}_q[x] \text{ monic, squarefree, } r\text{-additive of degree } r^d, C(f) = i\}.$$

Blüher gives formulas for $d = 2$. We demonstrate analogous formulae for $d = 3$, and discuss the problem for more general d . We also provide computable constructions and fast algorithms, requiring time polynomial in d and $\log q$. (Received September 14, 2011)