

1077-13-964

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Evansville, IN 47722. *A Generalization of Integer-valued Polynomials Rings.*

The classical ring of integer-valued polynomials  $\text{Int}(\mathbb{Z})$  consists of the polynomials in  $\mathbb{Q}[x]$  that map  $\mathbb{Z}$  into  $\mathbb{Z}$ . In this talk, we consider a generalization of integer-valued polynomials where the polynomials act on  $\mathbb{Z}$ -algebras such as a ring of algebraic integers or the ring of  $n \times n$  matrices with entries in  $\mathbb{Z}$ . Specifically, given a  $\mathbb{Z}$ -algebra  $A$ , we define  $\text{Int}_A(\mathbb{Z})$  to be the set of polynomials in  $\mathbb{Q}[x]$  that map  $A$  into  $A$ ; then,  $\text{Int}_A(\mathbb{Z})$  is usually a proper subring of  $\text{Int}(\mathbb{Z})$ . The principal question we consider is whether or not  $\text{Int}_A(\mathbb{Z})$  is a Prüfer domain. We will demonstrate that when  $A$  is a finite-dimensional  $\mathbb{Z}$ -algebra,  $\text{Int}_A(\mathbb{Z})$  need not be a Prüfer domain, but the integral closure of  $\text{Int}_A(\mathbb{Z})$  is always a Prüfer domain. (Received September 14, 2011)