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Tomer M. Schlank* (tomerschlank@gmail.com) and **Yonatan Harpaz**
(harpazy@gmail.com). *Homotopy Obstructions to Rational Points - I.*

In 1969 Artin and Mazur defined the étale homotopy type $\hat{E}t(X)$ of a scheme X as a way to homotopically realize the étale topos of X . In this talk we will consider the relative situation $X \rightarrow S$ and define a relative version $\hat{E}t/S(X)$ of this notion. We call it the **relative homotopy type of X over S** .

It turns out that the relative homotopy type can be especially useful in studying the sections of the map $X \rightarrow S$. In particular this notion can be used in order to obtain homotopy-theoretic obstructions to the existence of a section.

In the special case where $S = \text{Spec}(K)$ is the spectrum of a field K , the set of sections are just the set of K -rational points $X(K)$. In that case the obstructions we obtain are a direct generalization of Grothendieck's section obstruction. If furthermore K is a **global field** then these obstructions can be used to describe various known arithmetic obstructions, such as the regular and étale Brauer-Manin obstructions. This point of view can be used to show new properties of these obstructions. (Received September 21, 2011)