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A frame is a redundant spanning set. A tight frame is a generalization of an orthonormal basis. A notion of digram vectors associated to frames in  $\mathbb{R}^2$  has yielded many results about tight frames in  $\mathbb{R}^2$ . We provide a generalized notion of diagram vectors which allows for significant developments in the theory of tight frames in finite dimensions. In particular, we completely answer the *tight frame scaling problem* - that is, given a set of unit vectors  $\{f_i\}_{i=1}^k$  in a finite dimensional Hilbert space  $\mathcal{H}_n$ , when do there exist positive scalars  $c_1, \dots, c_k$  so that  $\{c_i f_i\}_{i=1}^k$  is a tight frame? When such scalings do exist, we provide a means of determining coefficients using a specific formulation for  $\mathbb{R}^2$  as well as a general approach for  $\mathcal{H}_n$  using techniques from computational geometry. (Received July 28, 2011)