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11225. *The invariant Hilbert scheme of a spherical module.* Preliminary report.

Let G be a complex connected reductive linear algebraic group and let V be a finite-dimensional G -module. The invariant Hilbert scheme $\text{Hilb}_h^G(V)$, introduced by V. Alexeev and M. Brion, parametrizes the G -stable ideals I of the polynomial ring $\mathbb{C}[V]$ for which the G -module $\mathbb{C}[V]/I$ has prescribed multiplicities given by a function $h : \text{Irr}(G) \rightarrow \mathbb{Z}_{\geq 0}$.

Suppose W is a *spherical* G -module (i.e. $\mathbb{C}[W]$ is a multiplicity-free G -module) and denote $h_W : \text{Irr}(G) \rightarrow \{0, 1\}$ its *invariant Hilbert function*, so that $\mathbb{C}[W] \cong \bigoplus_{M \in \text{Irr}(G)} M^{h_W(M)}$ as a G -module. Let $T \subset G$ be a maximal torus and let $U \subset G$ be a maximal unipotent subgroup normalized by T . There is a (unique) finite-dimensional G -module V such that $\mathbb{C}[W]^U \cong \mathbb{C}[V^U]$ as T -modules. We will discuss our work on the invariant Hilbert scheme $\text{Hilb}_{h_W}^G(V)$, which provides information on the equivariant degenerations of W . (Received September 16, 2011)