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Igor A. Rapinchuk*, Yale University, Department of Mathematics, 10 Hillhouse Avenue, New Haven, CT 06511. *On the conjecture of Borel and Tits for abstract homomorphisms of algebraic groups.*

The conjecture of Borel-Tits (1973) states that if G and G' are algebraic groups defined over infinite fields k and k' , respectively, with G semisimple and simply connected, then given any abstract representation $\rho: G(k) \rightarrow G'(k')$ with Zariski-dense image, there exists a commutative finite-dimensional k' -algebra B and a ring homomorphism $f: k \rightarrow B$ such that ρ can essentially be written as a composition $\sigma \circ F$, where $F: G(k) \rightarrow G(B)$ is the homomorphism induced by f and $\sigma: G(B) \rightarrow G'(k')$ is a morphism of algebraic groups. We prove this conjecture in the case that G is either a universal Chevalley group of rank ≥ 2 or the group $\mathbf{SL}_{n,D}$, where D is a finite-dimensional central division algebra over a field of characteristic 0 and $n \geq 3$, and k' is an algebraically closed field of characteristic 0. In fact, we show, more generally that if R is a commutative ring and G is a universal Chevalley-Demazure group scheme of rank ≥ 2 , then abstract representations over algebraically closed field of characteristic 0 of the elementary subgroup $E(R) \subset G(R)$ have the expected description. We also give applications to deformations of representations of $E(R)$. (Received August 14, 2011)