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Paul Frank Baum* (baum@math.psu.edu), Department of Mathematics, Penn State University, University Park, PA 16802. *Geometric Structure in the Representation Theory of Reductive p-adic Groups.*

Let G be a reductive p -adic group. Examples are $GL(n, F)$ $SL(n, F)$ where n can be any positive integer and F can be any finite extension of the field Q_p of p -adic numbers. The smooth (or admissible) dual of G is the set of equivalence classes of smooth irreducible representations of G . The representations are on vector spaces over the complex numbers. The smooth dual has one point for each distinct smooth irreducible representation of G . Within the smooth dual there are subsets known as the Bernstein components, and the smooth dual is the disjoint union of the Bernstein components. This talk will explain a conjecture due to Aubert-Baum-Plymen (ABP) which says that each Bernstein component is a complex affine variety. These affine varieties are explicitly identified as certain extended quotients. The infinitesimal character of Bernstein and the L-packets which appear in the local Langlands conjecture are then described from this point of view. Recent results by a number of mathematicians (e.g. V. Heiermann, M. Solleveld) provide positive evidence for ABP. (Received July 24, 2011)