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Robert A Bridges* (bridges@purdue.edu). *Schroeder's Equation in Several Variables.*

If $\phi : \mathbb{D} \rightarrow \mathbb{D}$ is analytic fixing 0, Schroeder's equation asks one to find an analytic f and $c \in \mathbb{C}$ satisfying

$$f \circ \phi = cf.$$

In 1884 Koenigs showed that there is such an f , which is bijective near 0, if and only if $c = \phi'(0) \neq 0$. If C_ϕ is the composition operator sending g , a function defined on \mathbb{D} , to $g \circ \phi$, Koenig's solution gives an eigenvector & value of C_ϕ . Additionally, it is a first step in understanding intertwining maps and models of iteration which have been a fruitful approach for composition operators.

The overall goal is to find such a model for iteration with domain \mathbb{B}^n .

In 2003 Cowen and MacCluer formulated a several variables Schroeder's equation. Let \mathbb{B}^n be the unit ball in \mathbb{C}^n , and $\phi : \mathbb{B}^n \rightarrow \mathbb{B}^n$ analytic, fixing 0, $\phi'(0)$ full rank, and $|\phi(z)| < |z|, z \neq 0$. Does there exist an analytic $F : \mathbb{B}^n \rightarrow \mathbb{C}^n$ so that

$$F \circ \phi = \phi'(0)F?$$

This talk will give necessary and sufficient conditions for a solution. (Received September 01, 2011)