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There is essentially a one to one correspondence between pseudo-spherical immersions in \mathbb{R}^3 , Lorentz harmonic maps to S^2 and solutions to the sine-Gordon equation $\omega_{xy} = \sin \omega$. All C^2 solutions to the sine-Gordon equation are given by a loop group factorization process whose input are assumed to be C^1 . What happens if the input is only C^0 ? It turns out that one still obtains a C^1 solution to the sine-Gordon equation. That is ω_{xy} and ω_{yx} exist, are equal, and also equal $\sin \omega$.

Hilbert proved that there are no C^2 pseudo-spherical immersions of \mathbb{R}^2 into \mathbb{R}^3 using basic properties of the sine-Gordon equation. On the other hand Kuiper proved there exist such C^1 immersions, however no examples are known. We will review the loop group constructions, sketch proofs of the claims, hopefully show some graphics and discuss open questions. (Received September 22, 2011)