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Correspondences between ideals and z -filters for rings of continuous functions between C^ and C .*

Let X be a completely regular topological space and let $A(X)$ be any ring of continuous functions satisfying $C^*(X) \subseteq A(X) \subseteq C(X)$. We show that the correspondence \mathcal{Z}_A (defined in Redlin, L. and Watson, S.; Maximal ideals in subalgebras of $C(X)$, *Proc. Amer. Math. Soc.* **100** (1987), 763–766) between ideals of $A(X)$ and z -filters on X extends the well-known correspondence for $C^*(X)$ to any $A(X)$. We also define a new correspondence \mathfrak{Z}_A that extends the well-known correspondence for $C(X)$ to any $A(X)$. In addition, we show that \mathfrak{Z}_A is a one-to-one correspondence between the maximal ideals of any $A(X)$ and the z -ultrafilters on X , and we give an explicit formula that relates the correspondences \mathcal{Z}_A and \mathfrak{Z}_A . We use properties of \mathcal{Z}_A and \mathfrak{Z}_A to characterize $C^*(X)$ and $C(X)$ among intermediate rings on X . For rings $A(X)$ that are C -rings, we use the map \mathfrak{Z}_A to give a topological characterization of the maximal ideals in any $A(X)$ that generalizes the Gelfand-Kolmogoroff characterization of maximal ideals in $C(X)$. (Received September 22, 2011)