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Thomas Albert Laetsch* (tlaetsch@math.ucsd.edu), 9500 Gilman Dr #0112, La Jolla, CA 92037-0112. *An L^2 metric limit theorem for Wiener measure on manifolds with non-positive sectional curvature.*

An interpretation is given for the informal path integral expression

$$\frac{1}{Z} \int_{\sigma \in H(M)} f(\sigma) e^{-E(\sigma)} \mathcal{D}\sigma,$$

where Z is a "normalization" constant and $H(M)$ is the collection of paths on M with energy $E(\sigma) < \infty$. Given an equally spaced partition, \mathcal{P} , of $[0, 1]$, we let $H_{\mathcal{P}}$ be the finite dimensional manifold consisting of piecewise geodesic paths adapted to \mathcal{P} , which is given the L^2 metric, G . It is proved that

$$\frac{1}{Z_{\mathcal{P}}} e^{-\frac{1}{2}E(\sigma)} d\text{Vol}_G(\sigma) \rightarrow \exp\left(-\frac{1}{10} \int_0^1 \text{Scal}(\sigma(s)) ds\right) d\nu(\sigma)$$

where $Z_{\mathcal{P}}$ are appropriate normalization constants and ν is the Wiener measure associated to M . (Received September 22, 2011)