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Recent work is presented on the problem of computing sparse multiples of polynomials over the rational numbers or a finite field. Specifically, given a (dense) polynomial  $f \in \mathbb{F}[x]$ , we look for another polynomial  $g \in \mathbb{F}[x]$  with  $f|g$ , such that  $g$  has higher degree but fewer nonzero terms than  $f$ . Depending on the field  $\mathbb{F}$ , a bound on the degree of the multiple  $g$ , or on the coefficient sizes, is also required.

This problem has important applications in cryptography and extension field arithmetic. Though a few heuristic approaches have previously been developed, our interest is in the existence or nonexistence of polynomial-time algorithms in the *size* of the polynomials (that is, the number of nonzero terms, the logarithm of degree, and the size of the coefficients). We provide such polynomial-time algorithms for certain cases, and prove NP-hardness in other cases.

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